

Testing the fairness of citation indicators for comparison across scientific domains: the case of fractional citation counts

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Citation numbers are extensively used for assessing the quality of scientific research. The use of raw citation counts is generally misleading, especially when applied to cross-disciplinary comparisons, since the average number of citations received is strongly dependent on the scientific discipline of reference of the paper. Measuring and eliminating biases in citation patterns is crucial for a fair use of citation numbers. Several numerical indicators have been introduced with this aim, but so far a specific statistical test for estimating the fairness of these numerical indicators has not been developed. Here we present a statistical method aimed at estimating the effectiveness of numerical indicators in the suppression of citation biases. The method is simple to implement and can be easily generalized to various scenarios. As a practical example we test, in a controlled case, the fairness of fractional citation count, which has been recently proposed as a tool for cross-discipline comparison. We show that this indicator is not able to remove biases in citation patterns and performs much worse than the rescaling of citation counts with average values.

PACS numbers:

I. INTRODUCTION

Recent years have witnessed an increasing use of citation numbers for the quantitative assessment of scientific research activities, and many countries have already established national research evaluation agencies whose judgment criteria are based mostly on citation numbers [1, 2]. The use of citation numbers for research evaluation has been criticized [3, 4], especially because the meaning of citations may be strongly context dependent [5]. As a matter of fact, however, citations play a crucial role in modern science, and often important decisions such as the granting of research funds [6] or institutional positions [7] are heavily influenced by numerical indicators based on citations.

Generally speaking, citations are interpreted as proxies for the impact or influence of papers in the scientific community. That is, the more citations a paper has accumulated, the more relevant this paper can be considered for its own scientific community of reference. Citation numbers, however, are not only used for the quantitative evaluation of scientific publications, but also for the formulation and quantification of numerical indicators devoted at the assessment of the career of scholars [8, 9] and the quality of scientific journals [10]. Sometimes the use of citation numbers is also extended to the judgment of departments [11, 12], of institutions [13] and even of entire countries [14].

A fundamental problem in citation analysis is the presence of biases in citation numbers. It is for example well known that papers in mathematics accumulate citations at a rate much lower than papers in, say, chemistry. It is therefore unfair to directly com-

pare citation numbers in mathematics and chemistry. Suitably modified indicators should instead be used in order to remove such patent bias among disciplines. If such biases are not removed then they can affect comparisons from the level of individuals up to research groups or institutions. While a direct comparison among scholars in different disciplines may seem not so common (although examples exist, see for example http://www.topitalianscientists.org/Top_italian_scientists.VIA-Academy.aspx) when departments, universities or scientific institutions are compared, as it often occurs, this problem is unavoidable and potentially very dangerous. The lack of a proper handling of this bias may make those comparisons almost pointless.

Slightly less severe, the problem of different citation patterns also exists for different fields within the same discipline [15], where it is customary that citation records of scholars are compared in competitions for the same resources, such as academic positions or research grants. The problem of biases in citation numbers is therefore crucial, if not in cross-disciplinary comparisons, in comparisons among sub-fields or topics of research within the same scientific domain.

Several studies have dealt with this issue [16–19]. The common idea is the development of normalized indicators (i.e., the raw number of citations is divided by a discipline dependent factor) able to suppress discrepancies among scientific domains. (For other approaches see [20, 21]). Independently of the particular recipe proposed, these studies do not generally provide a quantitative test able to determine whether their proposed method is able to

effectively suppress citation biases or not ¹.

One of the problematic issues for rescaled indicators is the attribution of papers to disciplines. This categorization is usually derived from an existing (and questioned) attribution of journals to disciplines: if a paper appears in a journal it is assumed to belong to the same category (or categories) the journal belongs to. This procedure has several obvious potential inconvenients [23]. To overcome this problem, Leydesdorff and Opthof [24] have recently proposed an indicator based on a fractional citation count [25], i.e., weighting each citation as $1/n$, where n is the total number of references in the citing paper. Assuming that differences between citation patterns across domains are due to different typical lengths in reference lists, this method provides an implicit normalization of citation counts that does not require any explicit classification of papers into categories.

In this paper, we contribute to the search for effective ways to remove the bias in two ways.

First, we propose a general method for testing the effectiveness of numerical indicators aimed at the removal of biases in citation counts among scientific domains. The method relies on a simple selection process and compares the values of the indicator under test with those expected under the hypothesis that the indicator is not biased. Indicators able to suppress citation biases should produce results statistically consistent with an unbiased selection process, while their failure in the test directly indicates their non-effectiveness in the suppression of biases.

Secondly, as a practical application, we apply the method to two recently proposed normalization schemes for paper citation counts. We consider a large database of physics papers, which has the important feature that the attribution of papers to categories is directly provided by authors and thus can be considered to be accurate. In this way the categorization step is not a potential source of problems. We show that, while the rescaled indicator of Radicchi et al. [26] effectively allows an unbiased comparison among different sub-fields, the fractional citation count of Leydesdorff and Opthof [24] largely fails the same test and does not constitute a substantial improvement over raw citation numbers.

We would like to stress that our notion of “fairness” is based on the strong assumption that each discipline or field of research has the same importance for the development of scientific knowledge. According to our assumption, a “fair” numerical indicator based on citation numbers assumes values that do not depend on the particular scientific domain taken under consideration. It is clear

that our notion of fairness strongly depend on the classification of papers into categories (disciplines, fields, topics). Also it is important to remark that other possible definitions of fairness could be stated without relying on the assumption that each discipline or research field has the same weight for scientific development.

II. MATERIAL AND METHODS

We consider all papers published in journals of the American Physical Society (APS, www.aps.org) between years 1985 and 2009. The *xml* file containing all the relevant information about publications in APS journals up to 2009 was directly provided by the editorial office of APS

(<http://publish.aps.org/datasets-announcement>).

We restrict our analysis only to standard research publications (Letters, Rapid communications, Brief Reports and Regular Articles) and exclude other type of published material (Editorials, Reviews, Comments, Replies and Errata) which may show distinct citation patterns. The journals considered in our analysis are: Physical Review Letters, Physical Review A, Physical Review B, Physical Review C, Physical Review D and Physical Review E. APS journals are the most typical publication outlets in physics and cover all sub-fields of this discipline. They therefore represent an optimal benchmark for the study of citation patterns of publications within physics [27]. The classification of papers into distinct categories is provided by PACS numbers, which are alphanumeric codes denoting the topic discussed in the paper and are attributed to papers by authors themselves. PACS codes are composed of three fields *XX.YY.ZZ*, where the first two are numerical (two digits each) and the third is alphanumeric. For our purpose we consider only the first digit of the *XX* code, which provides a classification into very broad categories (<http://publish.aps.org/PACS>). Hence, for example, two papers with PACS codes 05.70.*Ln* and 02.50.2*r* both belong to the category 00, while a paper with PACS number 64.60.*Ht* is part of the category 60.

The first year of the temporal range of our analysis is 1985, because in that year PACS numbers started to be systematically used. We consider only papers classified according to the PACS codes, which are the vast majority (> 95% between 1985 and 2009, nowadays the selection by authors of at least one PACS number is compulsory at the submission stage) of all papers published in APS journals, for a total of 307,992 papers. In general, authors assign to a paper two or three PACS numbers. In our analysis, we classify papers only according to their principal PACS number. This set of articles represents our set of cited papers, and here we will study only the properties of the citations received by these papers. For this purpose, each article in the set of cited papers was also retrieved in the WebOfScience (WOS, www.isiknowledge.com) database. We collected several

¹ One of the few exceptions to this general trend is the statistical test performed by Leydesdorff and Bornmann [22] in order to check whether their normalization procedure is able to suppress discipline related biases in a novel formulation of the journal impact factor.

information, but mainly their unique WOS identification numbers and their total number of cites (i.e., the field “times cited”).

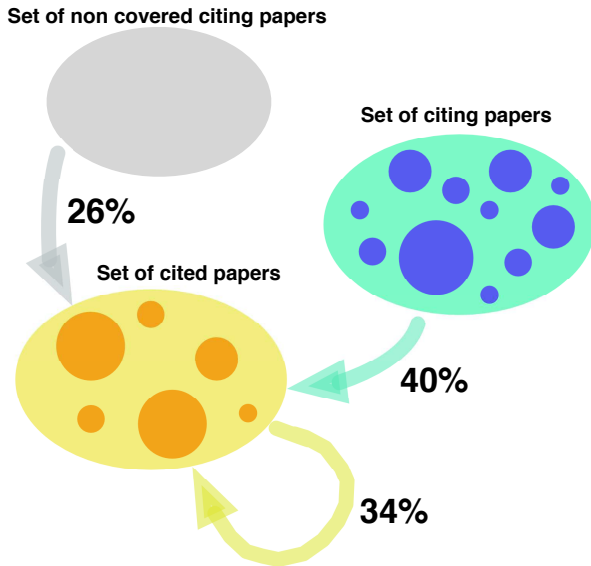


Figure 1: Schematic representation of the bibliographic dataset used in this paper. We focus our attention on the citation pattern of the set cited papers, which consists of all papers published in journals of the APS between years 1985 and 2009. Papers in the cited set are classified in research topics, according to their principal PACS number. The 34% of the citations received by the set of cited papers is originated by papers published between 1985 and 2011 in the same journals. We also consider an additional set of papers, published in other 139 scientific journals between 1985 and 2011, which cover an additional 40% of the total citations received by papers in the set of cited papers. The remaining 26% of the citations is not included in our analysis.

As set of citing papers, we first consider 349,285 papers published in the same journals as those belonging to the set of cited papers, but published between 1985 and the beginning of 2011. For each of these papers we obtain from WOS their list of references. In the reference list provided by WOS, cited papers are reported as unique WOS identification numbers. This information enables to match referenced papers with those belonging to the set of cited papers. With this first step, we are able to cover about the 34% of the total number of citations declared by WOS, calculated as the sum of all cites indicated in the field “times cited” of the set of cited papers. In order to increase the coverage of the set of citing papers, we collect also the list of references of 1,768,222 additional articles published in other 139 journals between 1985 and the beginning of 2011. These journals are selected because listed as top citing journals to the set of cited journals in the 2000 edition of Journal of Citation Reports (JCR) database. Please note that this list includes not only physics journals, but also chem-

istry, biology, engineering and multidisciplinary journals. The inclusion of this new set of citing articles enables us to cover about the 74% of the total number of citations received by the set of the cited papers (see Figure 1).

The entire data collection of cited and citing papers was performed between March 20 and March 29, 2011.

III. THEORY/CALCULATION

A. Normalization methods

We consider two normalization procedures which have been recently proposed for cross-discipline comparisons of paper citation counts by [24] and [26], respectively. The two schemes are conceptually different: in the former, citation weights are functions of the papers from which citations are originated; in the latter, citation weights are functions of the papers receiving citations. In the following, we provide detailed descriptions of both methods.

1. Fractional citation count

[24] have recently proposed a novel normalization scheme aimed at eliminating differences in citation counts among papers belonging to different scientific disciplines or about different topics. The method is based on the intuitive assumption that papers tend to cite other articles dealing with similar topics. The whole citation network is therefore organized into clusters of elements with reasonable high density of internal citations, while citations among different clusters are more rare. Under these assumptions, the average number of citations received by papers in a given compartment is proportional to the typical length of the reference list of articles published in that compartment. Papers in mathematics receive less citations than papers in biology because a typical paper in mathematics has a shorter reference list than a typical paper in biology. The method by [24], called “fractional citation count”, simply weights a citation from paper i to paper j as $1/n_i$, where n_i is the total number of articles referenced by paper i . In fractional citation count, the value \tilde{c}_j of the indicator for paper j is given by the sum of all citations received by paper j , where each citation is opportunely divided by the number of references of the citing paper

$$\tilde{c}_j = \sum_i \frac{A_{ij}}{n_i}, \quad (1)$$

where $A_{ij} = 1$ if paper i cites paper j , while $A_{ij} = 0$ otherwise.

The method has the great advantage that it does not formally require any *a priori* classification of the papers into scientific domains. This is a great advantage in many situations, because obtaining a reasonable classification of papers is very often nontrivial. This method does not require any external information regarding the classification of papers in different classes, but, as the authors claim, fractional citation counts “automatically” include the typical feature of the citation pattern of the cited papers. The practical disadvantage of the method is however the necessity of considering the whole list of citing papers, which may be difficult to retrieve.

The method has been already applied to the evaluation of departments in universities [23], to a new estimation of the impact factor of scientific journals [22, 28], and to a novel formulation of the *h*-index [28]. Similarly, the indicators developed by Zitt and Small [29] and Moed [30] for the assessment of the impact of scientific journals are based on a source normalization scheme for citations. The difference with respect to the indicator based on fractional citation count is, however, that the normalizing factor is not the exact length of the reference list of the citing paper, but instead the average length of the reference lists of all papers published in the same journal as the one of the citing paper. These studies propose interesting alternatives to the impact factor but also stress the inability of fractional citation count to well account for the degree of cross-field citations and the growth of the literature in a field of research.

2. Rescaled citation count

A different approach aimed at suppressing citation biases in cross-disciplinary comparisons is the one originally proposed by [31] and then considered also by [26]. Assuming that papers are classified in compartments corresponding to scientific disciplines and fixed years of publication, the authors showed that the only relevant difference in citation patterns corresponding to different compartments is the value of a single number c_0 , the average number of citations received by papers published in a given scientific discipline and in a given year of publication. By assigning to each paper a relative citation count indicator $c_f = c/c_0$ defined as the total number of cites c received by the paper divided by the value of c_0 corresponding to the category and year of publication of the paper, [26] were able to show that this quantity obeys a probability density function that is universal among scientific disciplines. The indicator based on rescaled citation counts thus provides a natural way of eliminating biases among scientific disciplines, since the probability to have a paper with relative indicator c_f equal to a certain value no longer depends on the particular discipline under consideration.

The practical disadvantage of the rescaled citation count indicator is related to the potential difficulties that may arise in the classification of papers in scientific disciplines.

In general, classifications are made at the level of scientific journals, and this may lead to some inconsistencies in the classification of papers. Journals belong to more than a scientific discipline if they publish papers about different subjects. Then, all papers published in these journals will belong to more scientific disciplines because their classification is based on the classification of the journals where they were published, but in reality each of these papers is just about a particular scientific subject and their multi-disciplinary feature is just an artifact of the classification procedure. On the other hand, the results of [26] show a very interesting and not trivial feature of the citation habits in science: apart from a typical citation scale, which is discipline dependent, the way citations accumulate is the same in all disciplines. More practically, the universal shape of the citation distribution (i.e., a lognormal distribution) allows to estimate the confidence intervals of the rescaled citation count indicator [32].

In the original paper, [26] analyzed 14 different scientific disciplines. The analysis has been recently extended to more complete datasets by [33] and [34], showing that in general the universality of the citation distribution holds in many scientific disciplines, with the notable exception of many social sciences [34]. Rescaled citation counts have been applied also to more refined contexts for the quantification of scientific relevance of papers in sub-topics within the same discipline: [35] focused their attention on papers published in chemistry journals, while [15] on papers published in journals of physics.

B. Fairness of the indicators

According to our definition, the value of a fair indicator associated to a paper should not depend on the particular category (topic of research or scientific discipline) of the paper. In other words, the probability of finding a paper with a particular value of a fair indicator must not depend on the topic/discipline of research of the paper, it must be the same across fields of research or scientific disciplines. The “fairness” of a citation indicator is therefore directly quantifiable by looking at the ability of the indicator to suppress any potential citation bias related to the classification of papers in disciplines or topics of research.

Based on these assumptions, here we propose a simple statistical test able to assess the fairness of a citation indicator. The procedure is very general and can be simply applied to any type of classification and/or any type of numerical indicator based on citations.

Imagine to have a set of N total papers divided in G different categories. Indicate with N_g the number of papers belonging to the g -th category. Each paper in the entire set has associated a score calculated according to the rules of the particular indicator we want to test. Imagine now to extract the top $z\%$ of papers from the whole set of papers. The list of the top $z\%$ papers in the dataset is

composed of the $n^{(z)} = \lfloor z N / 100 \rfloor$ papers with the highest values of the score ($\lfloor x \rfloor$ stands for the largest integer number smaller than or equal to x). If the numerical indicator is fair, the presence in the top $z\%$ should not depend on the particular category to which the paper belongs. That is, the presence of an article of the g -th category in the top $z\%$ should depend only on the number N_g of papers in category g , and not on the fact that papers in category g may be privileged for some other particular reason. Under these conditions, the number of papers $m_g^{(z)}$ in category g that are part of the top $z\%$ of the whole ranking is a random variate obeying the hypergeometric distribution ²

$$P\left(m_g^{(z)} \mid n^{(z)}, N, N_g\right) = \binom{N_g}{m_g^{(z)}} \binom{N - N_g}{n^{(z)} - m_g^{(z)}} / \binom{N}{n^{(z)}} \quad (2)$$

$\binom{x}{y} = x! / [y! (x - y)!]$ is a binomial coefficient which calculates the total number of ways in which y elements can be extracted out of x total elements. Eq. (2) describes a simple urn model [36], where elements (i.e., papers in our case) are randomly extracted from the urn without replacement. With this statistical model we can simply calculate the expected number of papers in category g present in the top $z\%$ as $E\left(m_g^{(z)}\right) = n^{(z)} N_g / N$. Moreover, we can make use of Eq. (2) for estimating confidence intervals or other relevant statistical quantities.

IV. RESULTS

We base our entire analysis on the bibliographic data set described in sec. II. A category here is therefore intended as the collection of all papers published in the same year and with the same first digit of the principal PACS number. This means that we have at our disposal a total of 250 different categories: 25 different years of publication and 10 different PACS numbers. We also stress once more that the analysis is based on the 76% of the total number of citations effectively accumulated by the papers in our set of cited papers. With our data, we are in fact not able to identify the source for the remaining 24% of the citations. This problem affects only the computation of the numerical indicator based on fractional citation counts, but for consistency we prefer to use the

same amount of information also for the computation of raw and rescaled citation counts.

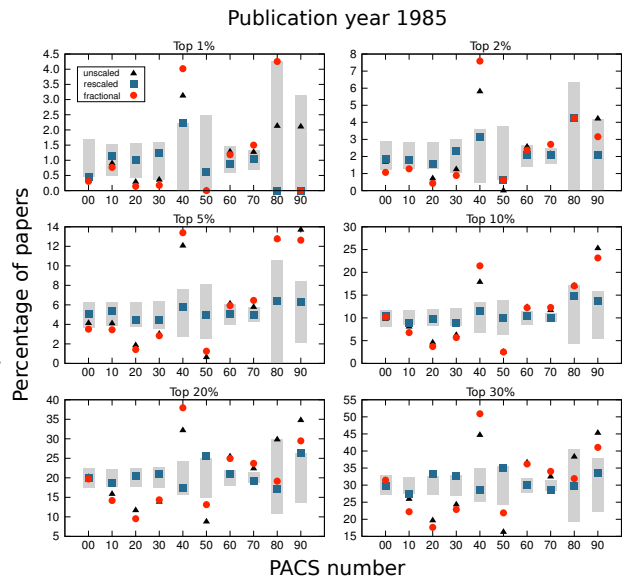


Figure 2: Percentage of papers belonging to the top $z\%$ for different PACS classification codes and different values of z . Here we consider only papers published in year 1985. Black triangles represent the results obtained with raw citation counts, blue squares stand for the results obtained with the indicator based on rescaled citation counts, while red circles indicate the results obtained using the indicator based on fractional citation counts. Gray areas bound the 90% confidence intervals and are calculated using Eq. (2). The values of the average number of citations c_0 and the number of papers N considered for each PACS code are: PACS 00 $c_0 = 32.73$ and $N = 655$, PACS 10 $c_0 = 29.48$ and $N = 783$, PACS 20 $c_0 = 21.30$ and $N = 703$, PACS 30 $c_0 = 25.71$ and $N = 564$, PACS 40 $c_0 = 58.75$ and $N = 224$, PACS 50 $c_0 = 18.13$ and $N = 160$, PACS 60 $c_0 = 39.48$ and $N = 1,014$, PACS 70 $c_0 = 37.99$ and $N = 1,734$, PACS 80 $c_0 = 46.04$ and $N = 47$, PACS 90 $c_0 = 57.00$ and $N = 95$.

In Figures 2 and 3, we report the percentage of papers associated to a particular PACS number that are present in the top $z\%$ of all papers published in a given year. We show the results only for papers published in years 1985 (Fig. 2) and 2000 (Fig. 3), but qualitatively similar results are obtained when we consider other publication years. In general, we see that the use of raw citation numbers causes clear disproportions among different subjects of research. Papers in “nuclear physics” (PACS 20) are underrepresented in the top percentage of papers, because papers in this sub-field of physics are typically less cited than papers in other sub-fields. On the other hand, papers in “astronomy & astrophysics” (PACS 40) overpopulate the set of highly cited papers. The proportion of papers belonging to this subject of research are typically two to three times larger than what expected on average in the case of an unbiased selection process. At the same time, the indicator based on fractional citation

² A more general treatment of the problem would require the use of the multivariate hypergeometric distribution

$$P\left(m_1^{(z)}, \dots, m_G^{(z)} \mid n^{(z)}, N, N_1, \dots, N_G\right) = \prod_{g=1}^G \binom{N_g}{m_g^{(z)}} / \binom{N}{n^{(z)}} ,$$

with $\sum_{g=1}^G m_g^{(z)} = n^{(z)}$ and $\sum_{g=1}^G N_g = N$. Here however, we perform only independent tests of fairness and consider one category at time.

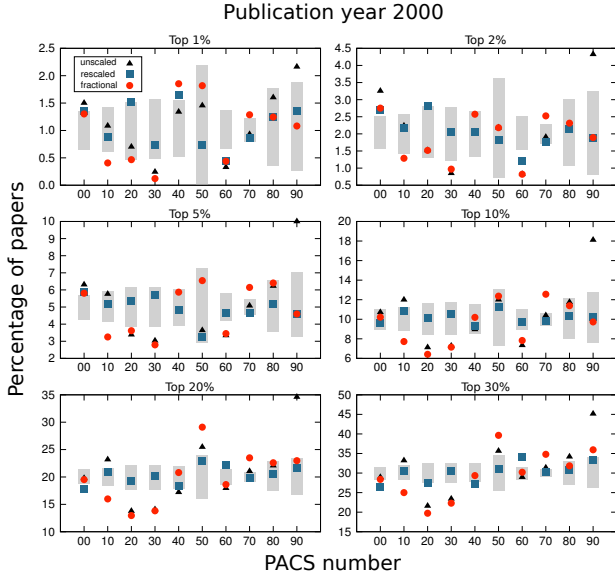


Figure 3: Same as Fig. 2, but for papers published in year 2000. The values of the average number of citations c_0 and the number of papers N considered for each PACS code are: PACS 00 $c_0 = 26.65$ and $N = 1,998$, PACS 10 $c_0 = 26.48$ and $N = 1,476$, PACS 20 $c_0 = 19.43$ and $N = 857$, PACS 30 $c_0 = 19.08$ and $N = 825$, PACS 40 $c_0 = 24.02$ and $N = 971$, PACS 50 $c_0 = 27.29$ and $N = 275$, PACS 60 $c_0 = 21.59$ and $N = 1,827$, PACS 70 $c_0 = 25.92$ and $N = 4,197$, PACS 80 $c_0 = 26.75$ and $N = 562$, PACS 90 $c_0 = 38.10$ and $N = 370$.

count still leads to “unfair” results. Some PACS numbers (the same as those privileged by raw citation counts) are favored, and the percentage of papers in these categories belonging to the top $z\%$ is much higher than what can be predicted (higher than the value corresponding to the 95% confidence interval). Conversely, other PACS numbers are underrepresented and their percentage is lower than the 5% confidence bound. The indicator based on rescaled citations, on the other hand, works pretty well. The results obtained are in the majority of the cases compatible with the statistical model of Eq. (2). The result holds for almost all PACS numbers and does not depend on the number of papers belonging to the PACS.

The same results can be understood in a more intuitive manner by looking at Figures 4 and 5. The cumulative distributions, relative to different PACS numbers, of the indicator based on fractional citation count do not collapse on top of each other. There is in general a systematic bias, and papers published under a particular PACS number have associated larger values of the indicator. The presence of a bias is particularly evident in the top left panel of Fig. 4. Here, we consider only papers published in 1985 and report the cumulative distribution for PACS numbers 00, 20, 40, 60 and 80. The indicator based of fractional citation counts is constantly larger for papers published under PACS 40, followed by those belonging to PACS 80, 60, 00 and 20.

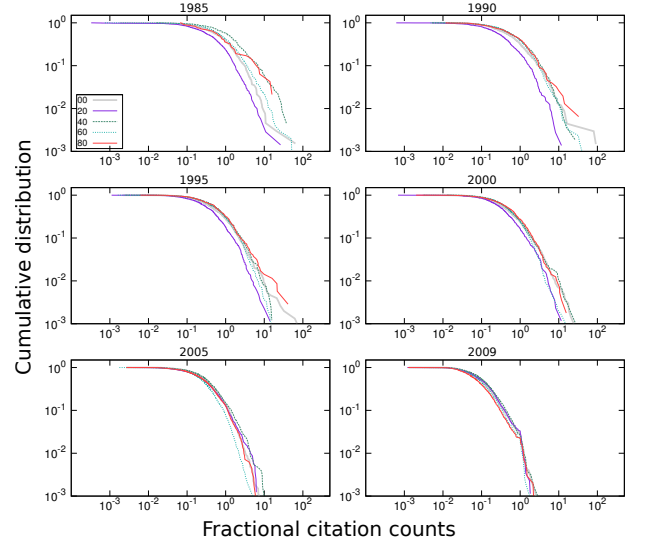


Figure 4: Cumulative distribution of fractional citation counts for different PACS numbers and year of publication.

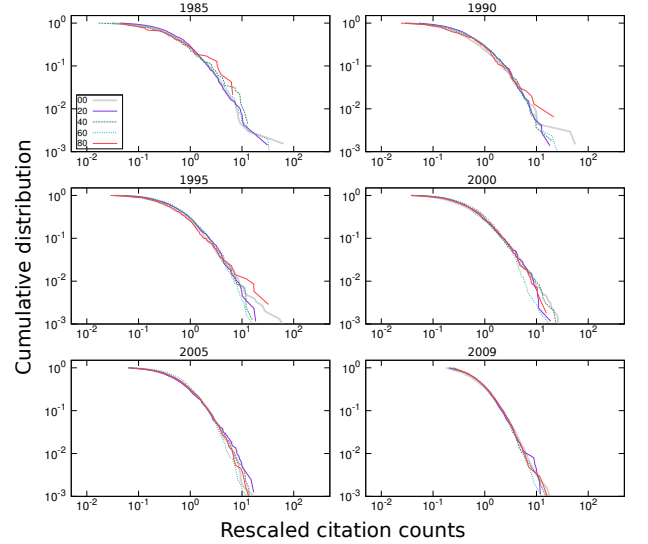


Figure 5: Cumulative distribution of the rescaled number of citations for different PACS numbers and year of publication.

The same systematic shift is not visible in the equivalent plots obtained with rescaled citations (Fig. 5). In this case, the curves corresponding to different PACS numbers overlap in a consistent way: Rescaled citations do not favor any particular field.

A quantitative measure summarizing the global performance of the different indicators is presented in Table I. We calculate, for all 250 sets under consideration (identified by the principal PACS number and the publication year), the percentage of categories for which the fraction of papers in the top $z\%$ falls within the 90% confidence interval of the distribution in the hypothesis that the indicator is not biased. It turns out that the rescaled citation count fully removes the bias for values of z up to

z	Rescaled citations	Fractional citations	Raw citations
1	88%	61%	60%
2	90%	56%	50%
5	92%	49%	41%
10	92%	48%	37%
20	79%	40%	33%
30	67%	34%	30%

Table I: Fraction of all categories for which the number of papers belonging to the top $z\%$ falls within the 90% confidence interval denoted by the gray areas in Figs. 2 and 3.

10%, while fractional citation count perform much worse (and only marginally better than raw citations).

V. DISCUSSION AND CONCLUSIONS

The results presented in the previous section show that attributing to each citation a fractional weight equal to the inverse of the total number of references is not sufficient to remove the biases that make citation numbers large in some disciplines (or fields) and small in others. This conclusion has been obtained by defining a quantitative statistical procedure to test the fairness of generic numerical indicators for the impact of papers and applying it in a controlled case. Our notion of fairness is based on the assumption that each scientific discipline contributes equally to the development of scientific knowledge, and therefore a fair numerical indicator based on citation counts should assume values that do not depend on the particular discipline taken under consideration. In this sense, fractional citation counts bring only a modest improvement with respect to the use of raw citation numbers. On the other hand it turns out that the rescaling of the number of cites with average values of the reference set is remarkably successful in removing biases. This indicator should then be used for a fair comparison of the impact of papers across disciplines.

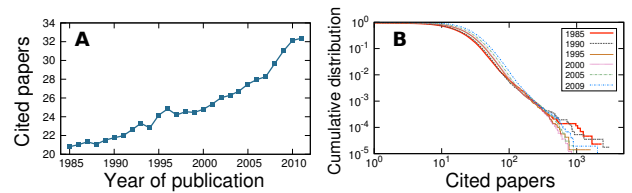


Figure 6: **(A)** Average number of cited papers as a function of the publication year of the citing article. **(B)** Cumulative distribution of the number of cited papers for different years of publication. Both figures are based on the set of citing articles, and numbers refer to their entire reference lists.

Counting citations fractionally is not an effective way to remove biases. Nevertheless, it would be very beneficial from a different point of view. As shown in Fig. 6A, which refer to the entire data set of citing articles, papers published in 1985 cited on average 21 other publications, while for papers published in 2011 the average length of the reference list exceeds 32. Even more striking is the shape of the distribution of the number of papers cited by a single publication (see Fig. 6B). The length of the reference list is very broadly distributed, with a non-negligible probability to observe papers citing thousands of documents. In practice this means that a single publication can contribute to citation numbers more than a hundred of others together. The large variability in the length of the reference lists is due to the heterogeneity of the type of citing documents. Short communications or letters, for example, are often subjected to length restrictions and therefore can cite only a limited amount of other papers. On the other hand, review articles have much longer lists of references which sometimes can be even two orders of magnitude larger than those of shorter documents. Nevertheless, the length of reference lists is growing with time, and some form of citing-side normalization would discourage the inflation of reference lists, thus making citation counts (in a different sense) more fair.

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- [1] N. Gilbert, *Quality of uk research assessed*, Nature News (2008).
 - [2] A. Abbott, Nature **460**, 559 (2009).
 - [3] M. H. MacRoberts and B. R. MacRoberts, J. Am. Soc. Inf. Sci. Tec. **40**, 342 (1989).
 - [4] R. Adler, J. Ewing, and P. Taylor, Stat. Sci. **24**, 1 (2009).
 - [5] L. Bornmann and H.-D. Daniel, J. Doc. **64**, 45 (2008).
 - [6] L. Bornmann, G. Wallon, and A. Ledin, PLoS ONE **3**, e3480 (2008).
 - [7] L. Bornmann and H.-D. Daniel, Scientometrics **68**, 427 (2006).
 - [8] J. E. Hirsch, Proc. Natl. Acad. Sci. USA **102**, 16569 (2005).
 - [9] L. Egghe, Scientometrics **69**, 131 (2006).
 - [10] E. Garfield, J. Amer. Med. Assoc. **295**, 90 (2006).
 - [11] P. Davis and G. F. Papanek, Am. Econ. Rev. **225** (1984).
 - [12] L. Leydesdorff and J. C. Shin, J. Am. Soc. Inf. Sci. Tec. **62**, 1146 (2011).
 - [13] A. L. Kinney, Proc. Natl. Acad. Sci. USA **104**, 17943 (2007).
 - [14] D. A. King, Nature **430**, 311 (2004).
 - [15] F. Radicchi and C. Castellano, Phys. Rev. E **83**, 046116 (2011).
 - [16] A. Schubert and T. Braun, Scientometrics **9**, 281 (1986).
 - [17] A. Schubert and T. Braun, Scientometrics **36**, 311 (1996).
 - [18] P. Vinkler, Scientometrics **36**, 223 (1996).
 - [19] P. Vinkler, Scientometrics **58**, 687 (2003).

- [20] L. Bornmann, J. Informetr. **4**, 441 (2010).
- [21] L. Leydesdorff, L. Bornmann, R. Mutz, and T. i. Opthof, J. Am. Soc. Inf. Sci. Tec. **62**, 1370 (2011).
- [22] L. Leydesdorff and L. Bornmann, J. Am. Soc. Inf. Sci. Tec. **62**, 217 (2011).
- [23] P. Zhou and L. Leydesdorff, J. Informetr. **5**, 360 (2011).
- [24] L. Leydesdorff and T. Opthof, J. Informetr. **4**, 644 (2010).
- [25] H. Small and E. Sweeney, Scientometrics **7**, 391 (1985).
- [26] F. Radicchi, S. Fortunato, and C. Castellano, Proc. Natl. Acad. Sci. USA **105**, 17268 (2008).
- [27] S. Redner, Phys. Today **58**, 49 (2005).
- [28] de Andrés, A., Europhys. News **42**, 29 (2011).
- [29] M. Zitt and H. Small, J. Am. Soc. Inf. Sci. Tec. **59**, 1856 (2008).
- [30] H. F. Moed, J. Informetr. **4**, 265 (2010).
- [31] J. Lundberg, J. Informetr. **1**, 145 (2007).
- [32] C. Castellano and F. Radicchi, Arch. Immunol. Ther. Ex. **57**, 85 (2009).
- [33] P. Albarrán, J. Crespo, I. Ortuño, and J. Ruiz-Castillo, Scientometrics **88**, 385 (2011).
- [34] L. Waltman, N. J. van Eck, and A. F. van Raan (2011).
- [35] L. Bornmann and H.-D. Daniel, J. Am. Soc. Inf. Sci. Tec. **60**, 1664 (2009).
- [36] H. M. Mahmoud, *Pólya Urn Models* (Chapman & Hall/CRC Texts in Statistical Science, 2008).